

Remaining Useful Life Prediction of Underground Water Pipes Using Design Expert

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Abstract—Remaining usable life (RUL) of water pipes can be categorized as history based, data dependent and physics-centered prediction models. A few authors developed hybrid RUL prediction models which calls for precise and trustworthy data. The purpose of this research is to create a mathematical model that uses secondary data to forecast RUL of underground water pipes. Response surface methodology (RSM) was employed to build the model to estimate the pipe RUL. A coefficient of determination R^2 value of 0.9876 was obtained after the model underwent response surface optimization, indicating that most of the variation in the dependent variable can be explained in the model for practical reasons. For practical reasons, the soil type, groundwater-table location and operational factors were not considered as the data can be used regardless of the environmental conditions.

Keywords— Coefficient of determination, Design of Experiments, Remaining useful life, Response Surface Methodology.

I. INTRODUCTION

Water pipes are essential components of a country's infrastructure since they are crucial for meeting humanity's most fundamental demand for water [1]. According to Tavakoli [2], the United States' water delivery system is thousands of miles long with pipes made of various materials, varying in size, age, and construction. These pipes are subjected to operational, structural, and physical stresses that eventually cause deterioration and failure. Given that degraded pipes are more vulnerable to leaks, pipe degradation is a fundamental factor in the detection of leaks. Since there is a time lapse between a pipe failure and its effects the failure are exceedingly difficult to diagnose [3]. The RUL of the mechanical system must be forecasted, specifically when the system is no longer performing reliably, due to the fact that most mechanical systems endure failure gradually ([4]). In accordance with [5], RUL forecasting is an approximation of the total amount of time that a system can still be used reliably, which is a crucial component of system health and the adoption of a robust maintenance strategy. RUL prediction models can be determined using the physics around the system, available data, and practical knowledge of the system. To create hybrid models, these models were combined by different authors.

The authors tested various combinations to create the best hybrid model. Forecasting the mechanical system's remaining useful life (RUL), particularly when it is no longer operating consistently, is necessary because most mechanical systems deteriorate gradually [4]. According to [5], RUL forecasting is an approximation of the total time that a system can still be reliably used, which is a very important aspect of system health and the adoption of a robust maintenance strategy. The physics surrounding the system, usage of the data at hand, and practical understanding of the system can all be used to determine RUL prediction models. Several writers integrated these concepts to create hybrid models. The authors tried different combinations in order to come up with the best hybrid model. Their conclusions were that a hybrid model can determine RUL more accurately as compared to using the models independently on the other hand, [6] proposed the use of genetic programming as a method to discover unconventional features that can determine the progression of RUL prediction. Their proposed methodology though, makes it difficult to interpret the physical meaning of the system degradation. [7] used Support Vector Regression-Particle Filter (SVR-PF) to forecast the remaining usable life of lithium-ion batteries. The prediction RUL model proposed provided the RUL quantity and updated the probability distribution of RUL to when the product is no longer usable. [8] developed a particle filter model with interacting multiple framework which used support vector regression so as to obtain multi-step-ahead approximation RUL of batteries.[9] suggested a prediction method that employed hot spot temperature method of prediction focusing on the functioning parameters of the transformer through the use of using a support that employs particle filter. In addition, an advanced particle filter (PF) approach was applied in the prediction of the RUL for bearings [9]. Particles at each iteration step were determined by a tunable significance density function, and a backpropagation (BP) neural network was applied to increase particle diversity before resampling.

A selection approach known as Adaptive First Predicting Time (FPT) was established by [10] for rolling elements bearings. The FPT was centered on 3σ interval in which particle filtering was applied to diminish random faults of the stochastic process. The process effectiveness was demonstrated through a replication and RUL prediction was done on four tests of bearing degradation. Furthermore, RUL prediction was done by, [11] though the use of a model-based method (a collective system) instead of a part of a machine. [12] used health indicator hinged on Recurrent neural network to forecast the RUL of bearings. [6], however, predicted the RUL of bearings by employing an integrated deep learning approach which combined both time and frequency domain features.

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II. DESIGN

A. Data collection

Secondary data was collected from a publication which was documenting RUL prediction of underground pipes by Tavakoli in 2018. In this investigation soil type, groundwater-table location and operational factors were not considered which therefore made it practical to use the data regardless of environmental conditions. Table 1 shows data that was used to determine the most significant parameters influencing RUL of underground water pipes.

TABLE I: STEEL PIPE LEAKAGE DATA SAMPLES (TAVAKOLI, 2018, PAGE NO 186)

| Mat | Age | Len | Dia | No | Wall | RUL |
|-------|-----|----------|-----|----|------|-----|
| Steel | 1 | 236 | 12 | 0 | 1 | 69 |
| Steel | 1 | 787.4 | 12 | 0 | 4 | 69 |
| Steel | 1 | 623 | 12 | 0 | 3 | 69 |
| Steel | 2 | 1,380 | 12 | 0 | 5 | 68 |
| Steel | 3 | 1,310 | 12 | 1 | 3 | 67 |
| Steel | 4 | 1,360 | 12 | 0 | 3 | 66 |
| Steel | 5 | 1,410 | 12 | 1 | 4 | 65 |
| Steel | 6 | 1,340 | 12 | 1 | 4 | 64 |
| Steel | 7 | 1,320 | 12 | 1 | 5 | 63 |
| Steel | 8 | 1,200 | 12 | 0 | 3 | 62 |
| Steel | 9 | 1,220 | 12 | 1 | 4 | 61 |
| Steel | 10 | 1,250 | 12 | 0 | 6 | 60 |
| Steel | 11 | 1,420 | 12 | 1 | 7 | 59 |
| Steel | 12 | 1,260 | 12 | 0 | 9 | 58 |
| Steel | 13 | 1,330 | 12 | 0 | 8 | 57 |
| Steel | 32 | 2,640 | 6 | 0 | 13 | 38 |
| Steel | 43 | 2,286.75 | 12 | 6 | 29 | 27 |
| Steel | 43 | 554.46 | 12 | 8 | 27 | 27 |
| Steel | 43 | 3,687.6 | 12 | 10 | 35 | 27 |
| Steel | 43 | 1,509 | 15 | 2 | 37 | 27 |
| Steel | 43 | 919 | 15 | 1 | 31 | 27 |
| Steel | 43 | 853 | 17 | 1 | 37 | 27 |
| Steel | 43 | 2,464 | 17 | 2 | 39 | 27 |

Where :Mat- Material, Age – Age in years, Len- Length in feet, Dia- Diameter in inches, No- Number of breaks, Wall – % Wall loss, RUL-Remaining useful life in years.

B. Design of Experiments Using Design Expert Software

Design expert 13 is a statistical software package that is used to perform design of experiments (DOE). DOE is a powerful tool for understanding and optimizing complex processes [13]. DOE assists in identifying very important variables and interactions that has an effect on RUL, allowing for more accurate and reliable predictions. For DOE using secondary data, RUL was defined as the response variable. The units and range of the RUL was set. The next step was to identify the input variables which, in this case, were the age, length and diameter of the pipe. These were the independent variables that affected the response variable. After defining the input variables, central composite design was identified to be used for the design of experiments. This design can identify the curvature of the response surface, and can provide insights into the optimal settings for the factors that maximize the RUL. Data was collected for each combination of input variables

defined in the experimental design. The collected data was analyzed and significant main effects and interactions between input variables that affect RUL were identified. The software generated statistical models that predicted RUL based on the input variables. The process was optimized using the statistical models generated by the software and the best conditions for maximizing RUL were identified. DOE using Design Expert software is a valuable tool for predicting RUL using secondary data. By identifying the most important input variables and their interactions, the accuracy of RUL predictions can be improved and the maintenance process can be optimized for maximum efficiency and effectiveness.

C. Response surface methodology (RSM)

RSM was employed to come up with a model to predict RUL. RSM is a statistical procedure that is usually employed to model and optimize complex systems. RSM forecasts and optimizes the RUL of water pipes centered on pipe age, diameter and length. Experiments were designed to collect data on the system's performance over time and statistical tools were used to analyze the data and develop a framework that predicts the RUL of the system using experimental variables.

The model was initially validated by comparing its predictions with actual RUL data from the system. The model was used to optimize the RUL by identifying the most important factors and adjusting them accordingly. The most important parameters were displayed from a correlation table generated from initial variables and responses that were entered into design expert software. The tabulated results show a correlation of -0.346 between RUL and age of the pipe. This meant the older the pipe the less the number of useful years remain for the pipe. There was however, a 0.787 degree of correlation between age and number of breaks which indicates a high degree of positive correlation. Thus as the age increases the number of breaks also increases. A moderately high positive correlation existed between age and wall loss as shown by the correlation coefficient of 0.590. The table, presented a somewhat low negative correlation between length and RUL with a value of -0.434. This implied that there were greater chances of reduced RUL on longer pipes. A very low correlation of 0.185 existed between the pipe length and the breaks that occurred on the pipe. The correlation between length and wall loss was almost negligible as represented by the correlation coefficient of 0.038. Thus the rate at which wall loss took place was not affected by the length of the pipe. The correlation of 0.383 between RUL and diameter was such that the bigger the diameter, the higher the RUL. With larger diameter, the number of breaks decreased by -0.139. A negative correlation factor of -0.363 existed between diameter and wall loss. There was, however, no correlation at all between age, length and diameter.

III. MATHEMATICAL MODEL

In generating a mathematical model, design expert (DE) software identified the most probable equation for the model and the actual values had to be used in order to determine how accurate the prediction model was. Model1 was the first model that was generated to predict RUL. In the model: A is the age, B

is the length and C is the diameter of the pipe.

$$RUL = 19.095 - 1.780A + 0.010B - 0.252C + 0.026A^2 \quad (1)$$

The predicted R² of -4.9637, which is the coefficient of determination generated by model 1 indicated that the model was a poor fit. A larger R² value indicates that the dependent variables variation can be explained by the independent variables in the model and is better at predicting the dependent variable figures founded on independent variables. The adequacy (Adeq) precision which measures how well the model can predict the response variable for new observations that were not used to build the model, was used in conjunction with R² and mean squared error, to approximate the performance of the model. The Adeq precision of 6.2494 was generated which indicated that the model could be useful in predicting new data. However, this model was discarded because of its poor R² value as shown in Fig. 1.

Influential observations were produced using Cook's distance which is a statistical measure used to identify and generate influential points in regression analysis. Points with high Cook's values may have significant impact on the regression results.

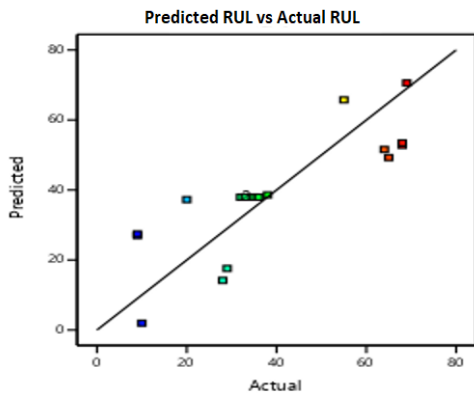


Fig. 1. Graph showing the predicted against the Actual RUL

In addition to Cook's distance, Design expert also provided leverage and studentized residuals, which helped in identifying influential points and other potential issues with the regression model. These diagnostic measures were used to refine the model and improve its predictive accuracy. In order to improve the model, observations number 2, 6, 9, 12, 18 and 20 which had Cook's distance that was greater than 0.2 (which is 4/20 and any point that is greater than 4/20 is an outlier), and the difference in fits (DFFITS) was either very low (-8.619) or very high (5.840). The removal of these influential observations helped in coming up with a better prediction model.

D. Reducing the Model

For a more significant model, model reduction was done by scrapping the results of the pipe aged 1, 2 and 61. The new values were entered into the Design Expert software for experimentation. Comparison with the first experiment were made and it was worth noting that the new model was also a quadratic model although a negative correlation of 0.979 was observed between age and RUL. This indicated age as the

parameter with the highest influence on RUL of underground water pipes. A moderately high positive correlation existed between age and the number of breaks, and age and the wall loss with correlation coefficients of 0.552 and 0.819 respectively. The reduced model had an F-value of 102.80 which showed a significant model. There was only a 0.01 probability of such a high F-value occurring because of noise. An insignificant lack of fit of 0.13 was observed on the reduced model as compared to model 1. A probability of 0.978 of such a high value of lack of fit can transpire due to noise. The reduced model is represented by Model 2 where: A is the age, B is the length and C is the diameter of the pipe.

$$RUL = 72.768 - 1.3A + 0.002B - 1.14C - 0.001AC + 0.009A^2 + 0.056C^2 \quad (2)$$

IV. RESULTS

From Table 2, R squared is 0.9893 which indicates that almost 99% of the total variation in RUL is explained by age, length and diameter of the pipe while the remaining percentage is due to other factors not included in the model. A predicted R² of 0.9776 was generated from model 2 which is in sync with a value of 0.9797 generated for adjusted R². There is a variation of smaller than 0.2 between the adjusted R² and predicted R² which indicating a good fitting model and is not overfitting the data. A 28.5577 Adeq precision value represents a high degree of accuracy in predicting new observations within the range of the design factors used in the experiment. It is calculated as the ratio of the range of predicted responses to the prediction error average.

TABLE II: FIT STATISTICS

| | | | |
|-----------|-------|--------------------------|---------|
| Std. Dev. | 1.99 | R ² | 0.9893 |
| Mean | 45.10 | Adjusted R ² | 0.9797 |
| C.V. % | 4.40 | Predicted R ² | 0.9776 |
| | | Adeq Precision | 28.5577 |

The Adeq precision is greater than the average prediction error by 28.5577 times, which suggest that the model is highly accurate in predicting new observations within the range of the design factors. A favorable and a better fit was produced when the RUL predicted was related to the real RUL as indicated in Fig 2. The graph shows no significant deviation of the RUL predicted RUL from the real RUL.

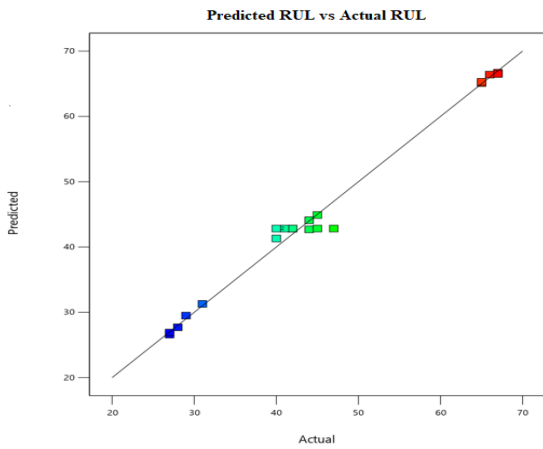


Fig. 2: Graph showing RUL predicted against the Real RUL of the cleaned up model

The relationship between age, length and the RUL of the pipe shown in Fig 3 which shows the response surface plot of age against length and length against RUL. From the surface plot, it is evident that age has very high influence on RUL as shown by the contour lines while the effect of length on RUL is almost negligible.

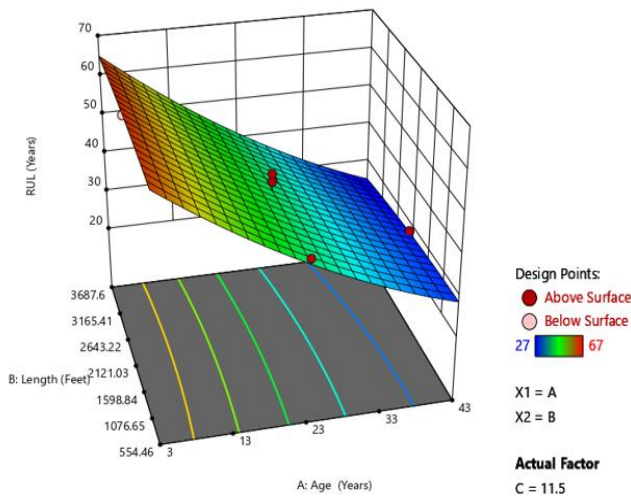


Fig. 3. Response Surface plot of RUL vs Age and Length.

Table 3 and 4 shows the points highlighted above the surface and below the surface of the response surface plot. The points highlight that even when the pipes are of the same length and have different ages the RUL will change significantly depending on the age.

TABLE III: RESULTS FROM ABOVE THE RESPONSE SURFACE PLOT.

| Age | length | RUL |
|-----|---------|-----|
| 23 | 2121.03 | 47 |
| 23 | 2121.03 | 45 |
| 23 | 554.46 | 44 |
| 28 | 211.03 | 28 |

TABLE IV: RESULTS FROM BELOW THE SURFACE.

| Age | length | RUL |
|-----|---------|-----|
| 23 | 3687.6 | 40 |
| 23 | 2121.03 | 41 |
| 23 | 2121.03 | 42 |
| 3 | 2121.03 | 65 |

A. Comparing the model with Actual RUL

RUL from the secondary data used was plotted against the RUL found from using the mathematical model and the results are shown graphically in fig 4, where the graphs have an almost similar trend.

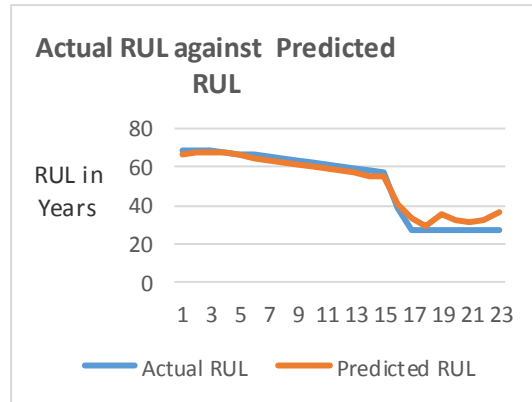


Fig. 4: Comparing the RUL predicted and the Real RUL

Fig 5 shows the trend line of the actual values generated from the scatter plot of the values of RUL predicted.

$$y = 0.7986x + 11.148 \tag{3}$$

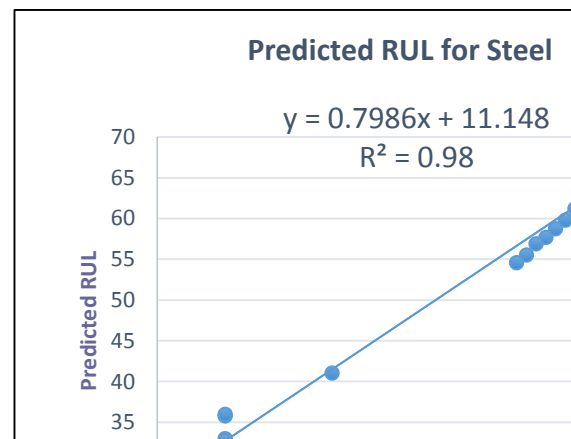


Fig. 5. Goodness of Fit for predicted RUL

From the graph, the predicted values of RUL do not deviate much from the trend line and a pattern can be seen from the set of data presented. This observation is supported by the trend line equation 3. The goodness of fit, R^2 , of 0.9876 shows that the data fit the regression model very well. The X-axis shows the actual RUL and the Y-axis presents the predicted RUL. Actual RUL was evaluated using the secondary data provided and forecasted RUL was calculated using the mathematical

model developed. The bulk of the figures shown are closer to $y=0.7986x+11.148$, and there is coefficient of determination of 99%. This very high coefficient of determination expresses that the developed mathematical model accurately foretold the pipe RUL of the pipeline and can be used reliably for extra investigation of the network.

V. MODEL VALIDATION

The model was validated using data on ductile iron from Tavakoli 2018. The pipe age of the data used for validation was from 10 years to 36 years with length ranging from 237 feet to 21120 feet.

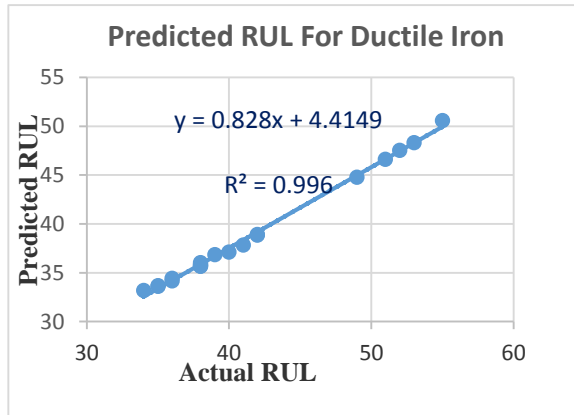


Fig. 6. Goodness of fit for prediction model on validation RUL

The diameter of the pipes used for validation was between 6 and 24 inches. Fig 6 shows the goodness of fit for the ductile iron actual RUL compared to the RUL predicted by the mathematical model developed. The X-axis shows the actual RUL while the Y-axis presents the predicted RUL.

VI. CONCLUSION

A mathematical RUL prediction model for underground water pipes was developed and validated. Age was seen to be the most significant parameter affecting RUL since a very high negative correlation exists between the age of the pipe and RUL. Response surface methodology further represented the results graphically to elaborate the relationship between age and RUL. The model created can be useful in forecasting RUL of pipes even when maintenance data is not available. Using the model enables a reliable health management system to be developed as scientific input will be used in determining the correct maintenance technique to be used.

VII. RECOMMENDATIONS

The accuracy of the model can be boosted by having more input parameters identified to have an effect on the water condition are available for modeling. Availability of primary data would help in coming up with a more accurate model as the soil type, groundwater-table location and operational factors would be considered for the prediction model.

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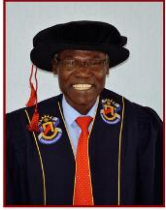
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